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Self-healing assessment of cementitious mortars through ultrasonic monitoring.

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Abstract: Self-healing cementitious composites have gained increased attention over the past decades, encouraged by the excessive costs related to manual concrete repair. Thorough investigations on these materials have shown their potential to be applied for real life construction elements. However, the existing methods used to assess the self-healing effectiveness possess several limitations, making an in-situ evaluation of the regained properties practically impossible. This study therefore investigates a non-destructive testing methodology based on ultrasonic wave propagation that can eventually be practically implemented. The sensitivity of ultrasound to the elastic properties of the material under study allows to assess the self-healing effectiveness and discriminate between actual healing, in the sense of mechanical properties restoration, and simple filling of the crack. Moreover, the method is validated and complemented by numerical wave simulations that allow to connect the macroscopically measured wave velocity to the stiffness of the healing products deposited within the crack.

Keywords: Cement; Self-Healing; Ultrasound; Wave simulations; Superabsorbent Polymer (SAP); hydrogel; Nanosilica.

1. Introduction

Since its first use in the mid-1800s, Portland-based concrete has become the most-used construction material. Due to its extensive usage, the maintenance and repair of concrete structures became equally important. However, manual repairs are costly, labour-intensive and limited by the accessibility of the structural element. For this reason, self-healing cementitious materials have attracted the attention of researchers around the world, which eliminate the previously mentioned issues and allow repairs to take place in a timely, automated manner. This process, called autogenous healing, allows to recover the water tightness (self-sealing) and to restore the mechanical performance (self-healing) of cracked elements. Autogenous healing consists of two main mechanisms, being the further hydration of unhydrated cement particles and the precipitation of CaCO_3 by the dissolution and carbonation of Ca(OH)_2 present inside the crack [1] [2]. These processes occur simultaneously, though the continued hydration mostly takes place at early age, when unhydrated cement is still available, while the precipitation of CaCO_3 becomes more prominent at later age [3]. It should be mentioned that for these chemical processes to occur, water is essential to be present inside the cracks. As a result, the promotion of autogenous healing can be accomplished by maintaining the humidity within the cracks, which is most commonly done by the addition of superabsorbent polymers (SAPs) [4] [5] [6]. As their name implies, SAPs are able to absorb large amounts of water. When present inside the crack,

39 the SAPs absorb water from the outer environment, thereby physically blocking the crack entrance, and retain this
40 moisture until the relative humidity decreases. The absorbed water is then released inside the crack and drives the
41 hydration of cement and the calcite precipitation. In addition to the above mentioned two healing processes, a third
42 autogenous healing mechanism includes the pozzolanic reaction of CH into CSH within aqueous media. In this case,
43 a pozzolanic source should be present within the matrix, which can be achieved by the addition of nanosilica. These
44 nanoparticles are mostly used to obtain improved mechanical properties and durability of cementitious materials
45 [7] [8] [9]. As nanosilica is a highly-reactive, pozzolanic material, it is capable to rapidly transform CH to CSH in
46 aqueous media, which contributes to the promotion of self-healing [10]. Moreover, previous investigations on the
47 combination of nanosilica and superabsorbent polymers in cementitious composites show their compatibility [11]
48 [12], meaning that the mixtures benefit from the inclusion of both additives as the macro pore formation by the
49 SAPs and corresponding possible decrease in mechanical properties can be enhanced by the increase in strength
50 caused by the nanosilica addition.

51 The use of SAPs and/or nanosilica within cementitious mixtures has clearly shown its potential for self-healing
52 purposes [3] [4] [6] [10] [13]. To evaluate the self-healing effectiveness, various testing techniques are available,
53 depending on the feature to be investigated. The visual crack closure can be studied by means of microscopic analysis
54 [14], but only provides information on the filling at the surface. Filling within the crack depth can be studied by X-
55 ray tomography [4] [15], but then again it does not provide any guarantee on a physical connection between the
56 crack walls. To assess the water tightness or self-sealing ability, water permeability tests are often used [16] [17].
57 Still, to determine the regained mechanical performance, mechanical tests are necessary [18]. The use of these
58 intrusive or destructive evaluation methods would be impossible for operational structures, while a confirmation of
59 the regained mechanical properties is necessary to ensure a structure's safety. These issues lead to the development
60 of a non-destructive testing protocol that allows for an estimation of the load-bearing capacity after healing.

61 A technique that has demonstrated promising results is ultrasonic wave monitoring. Ultrasound is sensitive to the
62 microstructural developments and the elastic properties of the material it travels through. In case of cementitious
63 materials, ultrasound has mainly been adopted to monitor the hardening process [19] [20], estimate the mechanical
64 properties [21] [22] [23], identify damage [24] [25] [26] and, more recently, also to monitor the repair and healing
65 process [27] [28] [29] [30] [31]. The latter study comprised the monitoring of the self-healing effectiveness through
66 surface wave measurements, which were able to distinguish between the uncracked, cracked and healed state, as
67 the wave velocity and amplitude decreased upon cracking and restored when healing products were formed inside
68 the crack. Still, a limitation of the method is that the studied wave parameters depend on the entire propagation
69 path, which includes both the cracked/healed zone and the intact mortar around. While the outcome provides
70 interesting information on the restoration during healing, the effect of the healed layer was not separated from
71 these results and thus the stiffness of the healing products was not determined. An evaluation of these elastic
72 properties will be crucial to assess the self-healing ability, since a stiff connection between the crack walls is essential
73 to obtain mechanical restoration. A means to achieve this objective is the use of numerical wave simulations that
74 offer the capacity to alter the elastic properties of the crack model under study and thus to examine the
75 correspondence between the macroscopically measured wave velocity and the stiffness of the healing material,
76 without being masked by the rest of the uncracked material between the sensors. Additionally, the effect of only
77 partially filled cracks can be studied, which is a valid assumption based on literature studies [32].

78 In this study, cementitious mixtures with and without SAPs and/or nanosilica were investigated. Apart from the
79 expected self-healing, the most important objective in this study is the estimation of the healing product's stiffness
80 through ultrasonic assessment. Elastic wave parameters, like ultrasonic wave velocity and attenuation, are measured
81 to qualitatively reveal restoration of the propagation path. The experimental trends are then combined with

82 numerical results in order to lead to the actual stiffness of the healing products for the first time, quantifying the
83 restoration of mechanical properties.

84

85 **2. Materials and methodology**

86 **2.1 Materials**

87 To study the effect of the different additives, four mortar mixtures were designed, being a reference mixture without
88 additives, a mixture with SAPs, a mixture with nanosilica and a mixture containing both SAP and nanosilica. The
89 cement used is Portland cement CEM I 52.5N Strong from Holcim. River sand 0/2 was added as small aggregate in
90 an amount of 2 to 1 with respect to the weight of the binder. The water-to-binder ratio was kept constant at 0.35.
91 Due to the relatively low amount of mixing water, a superplasticizer was added in an amount of 0.4% compared to
92 the binder weight to increase the workability. The superplasticizer used was MasterGlenium 51 (concentration 35%)
93 from BASF. Note that, as nanosilica acts as a binder, cement was replaced partially by nanosilica in the concerned
94 mixtures to maintain the binder quantity.

95 The type of superabsorbent polymer used is a copolymer of acrylamide and sodium acrylate. The SAP is produced
96 by bulk polymerization and provided by BASF. The particle size is equal to $100 \pm 21.5 \mu\text{m}$ in the dry state and can
97 swell up to a size of $257 \pm 55 \mu\text{m}$ in demineralized water [33]. Whereas generally larger sizes of SAPs are utilized to
98 promote self-healing, this SAP was chosen owing to the limited reduction of the compression strength noticed in
99 previous research [13]. Moreover, the self-healing capacity of cementitious mixtures including the SAP under study
100 demonstrated its beneficial effect [3] [13]. The amount of SAPs added was set at 0.2% by weight of the binder.
101 Additional water was added to the mortar mixtures with SAPs to account for their water uptake. By means of a flow
102 table test, following NBN EN 1015-3 [34], an identical workability of the reference and SAP mixture was obtained for
103 an additional amount of 26 grams of water per gram of SAP. The SAPs were added to the mixing bowl in the dry
104 state and the additional water was added together with the mixing water and dissolved superplasticizer.

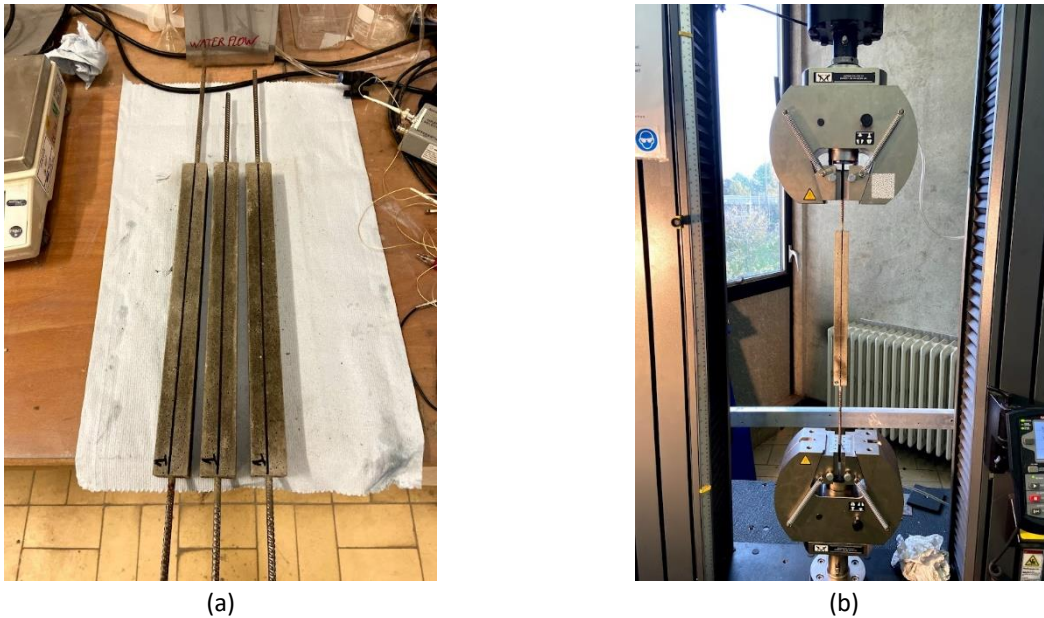
105 The nanosilica used within this study is a colloidal silica, namely LUDOX® HS40, and was obtained from W. R. Grace
106 & Co.-Conn (Antwerp, Belgium). The dispersion contains 40% of synthetic amorphous silica by mass. The nominal
107 diameter of the nanosilica particles is approximately equal to 12 nm and the specific surface area lies between 198
108 and 258 m^2/g . The amount of nanosilica amounts to 2% of the total weight of the binder and was chosen as it
109 counteracted the strength loss due to SAP inclusion, investigated in previous research [13]. In this way, the mortar
110 with SAPs and nanosilica has an identical compressive strength with respect to the reference material, which would
111 be important for future load-bearing purposes. Note that this amount refers to the dry silica particles and not to the
112 suspension. Mortar mixtures with nanosilica contained an increased amount of superplasticizer equal to 0.76%, as
113 the inclusion of nanosilica drastically lowered the workability. Superplasticizer was added instead of water, as the
114 nanosilica was unable to retain the water long enough to ensure an equal amount of mixing water during the
115 hydration stage. To improve the dispersion of the nanosilica particles, the colloidal solution was placed in an
116 ultrasonic bath for five minutes, prior to its addition to the cementitious blend.

117

118 **2.2 Sample preparation**

119 For every mixture composition, three mortar prisms measuring 30 mm x 30 mm x 360 mm were cast with a central
120 steel reinforcement bar of 6 mm diameter and a length of 700 mm, depicted in Figure 1 (a). It can be seen that a
121 central line was drawn, used for the positioning of the sensors during the healing assessment. The specimens were
122 cured in plastic foil for 28 days at $20 \pm 2^\circ\text{C}$. The cracking of the specimens was then executed by means of a tensile

123 test, using an Instron 5982 Floor Model Testing System with a capacity of 100 kN, as can be seen in Figure 1 (b). The
124 steel reinforcement was clamped within the testing device and a tensile load was exerted at a speed of 0.01 mm/s.
125 Due to the elongation of the steel bar, the mortar showed multiple cracking. On average six cracks were formed.
126 The test was continued until no new cracks appeared and an average crack width between 100 μm and 200 μm was
127 maintained after unloading.



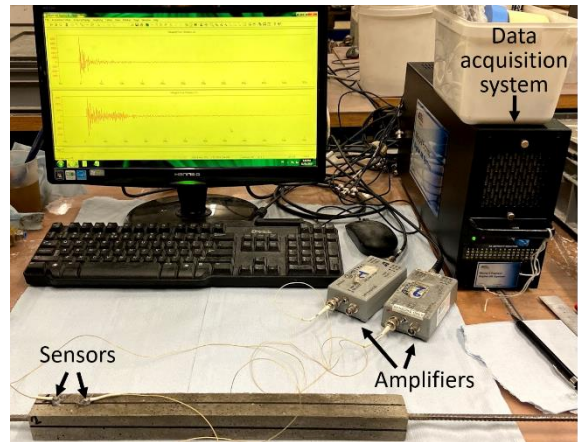
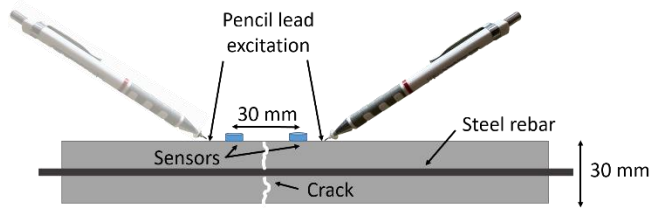
128 *Figure 1: Photographs of (a) the mortar specimens and (b) the tensile test set-up.*

129 After cracking, the specimens were placed in wet-dry curing cycles for 28 days to promote the crack healing
130 mechanism. The cycles consisted of 1 hour submersion in water at $20 \pm 2^\circ\text{C}$ and 23 hours of dry conditions at $20 \pm$
131 2°C and $65 \pm 5\% \text{RH}$.

132

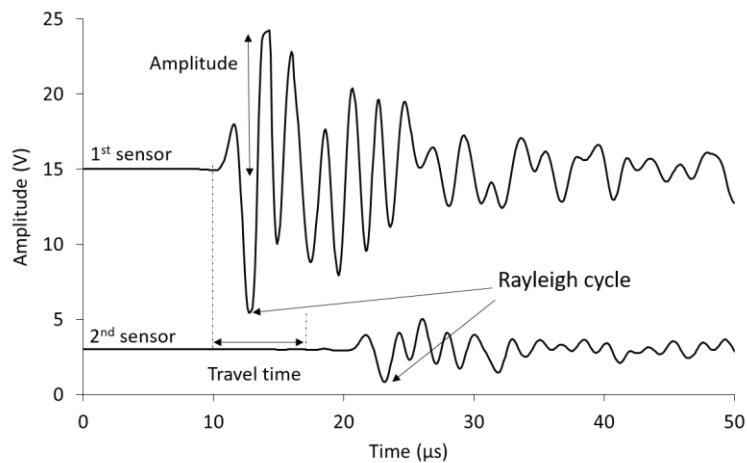
133 **2.3 Ultrasonic surface wave measurements**

134 The monitoring of the crack closure was performed by ultrasonic surface wave measurements. The set-up consisted
135 in the placement of two sensors on the surface of the specimen, at the position of the center line, using a thin layer
136 of vacuum grease as a coupling agent. The specific sensors (“pico” type) are relatively broadband sensors, operating
137 between 50 and 800 kHz. Their peak sensitivity lies at 450 kHz and their size is equal to 5 mm. The distance between
138 the sensors was 30 mm (center to center) in all experiments. The excitation of a wave signal was conducted by means
139 of mechanical pencil lead breaks. This is a standardized source, often used in literature, to produce broadband
140 excitations for ultrasonic measurements [35]. Every measurement was repeated five times, alternating the position
141 of the pencil; i.e. closer to the left or right sensor. A schematical representation of the test method can be seen in
142 Figure 2.



143 *Figure 2: Schematical representation of the ultrasonic surface wave measurements, showing the placement of the sensors and*
 144 *the pencil lead break test (left) and laboratory set-up (right).*

145 The assessment of the self-healing evolution was performed by an analysis of different wave parameters, namely
 146 the longitudinal wave velocity and the attenuation. In Figure 3, two waveforms received from a pencil lead break
 147 test on an intact mortar specimen are shown. The terms '1st sensor' and '2nd sensor' signify the closest and furthest
 148 sensor w.r.t. the pencil lead break, respectively. The first crossing of the threshold, defined as the maximum noise
 149 level of the received waveform during the "pre-trigger" stage, signifies the arrival of the longitudinal wave, which is
 150 by definition the fastest mode. Knowing the distance between the sensors, the longitudinal wave velocity can be
 151 calculated as the distance divided by the travel time between the sensors. For the example in Figure 3, a travel time
 152 6.6 μ s was found, leading to a velocity of 4545 m/s. Later, the arrival of the Rayleigh cycle can be distinguished by a
 153 more severe deviation of the amplitude from the noise level.



154
 155 *Figure 3: Typical waveforms received from a pencil lead break test on an uncracked mortar specimen.*

156 Apart from the wave velocity, attenuation provides important information on the propagation path. Attenuation is
 157 defined as the reduction in wave amplitude as the signal propagates a certain distance (between the two sensors).
 158 Scattering on aggregates and voids, cracks and damping within the matrix material contribute to the total amplitude
 159 loss. Looking at the example waveforms in Figure 3, the amplitude of the first sensor is equal to 9.24 V, whereas the
 160 amplitude at the second sensor is 2.05 V. The attenuation is calculated using Equation 1:

161
$$\text{Attenuation} \left[\frac{dB}{mm} \right] = -\frac{1}{D} * 20 * \log \left(\frac{A_2}{A_1} \right) \quad [1]$$

162 where A_1 and A_2 are the amplitudes in Volts of the closest and furthest sensor, respectively. D is the distance between
163 the sensors (30 mm in this case). An attenuation value of 0.44 dB/mm was obtained for the example case.

164 To monitor the self-healing evolution, this procedure was repeated at various moments within the wet-dry curing
165 cycles. At first, the uncracked state was evaluated after 28 days of curing in plastic foil. The specimens were then
166 cracked and from each specimen, one to two separated cracks were chosen to be followed-up by ultrasound. This
167 was done in order to eliminate any interaction of nearby cracks on the ultrasonic measurements, which could
168 provide immediate reflection of the emitted wave signal. The measurements took place immediately after cracking
169 and after 3, 7, 14 and 28 days of curing in wet-dry cycles. The steel reinforcement bars were wrapped with parafilm
170 to avoid possible corrosion. To eliminate the influence of the specimen's degree of saturation on the ultrasound
171 results, the tests were each time performed at the same moment within the curing cycles, being 16 hours after the
172 submersion in water.

173

174 2.4 Numerical simulations

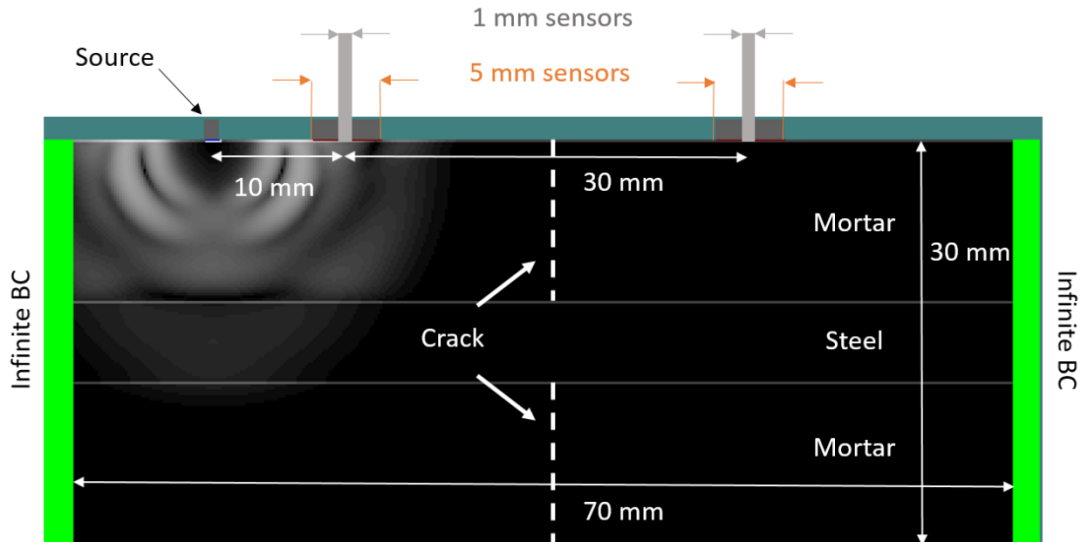
175 Numerical simulations were performed using the commercially available software Wave2000 Plus [36]. The software
176 utilizes a method of finite difference to solve the 2D elastic wave equations. The specific acoustic equation that is
177 simulated is:

$$\rho \frac{\partial^2 u}{\partial t^2} = \left(\mu + \eta \frac{\partial}{\partial t} \right) \nabla^2 u + \left(\lambda + \mu + \varphi \frac{\partial}{\partial t} + \frac{\eta}{3} \frac{\partial}{\partial t} \right) \nabla(\nabla \cdot u) \quad [3]$$

178

179 where u is the displacement vector (yielding two components u_x and u_y that are perpendicular to each other), t [s]
180 is the time, ρ [kg/m³] is the density, λ [Pa] is the first Lamé constant, μ [Pa] is the second Lamé constant, η [Pa·s] is
181 the shear viscosity and φ [Pa·s] is the bulk viscosity.

182 The simulated geometry is a two-dimensional representation of the experimental series and can be seen in Figure
183 4. The length of the specimen was limited to 70 mm instead of the 360 mm of the mortar samples, while infinite
184 boundary conditions were implemented at the edges to omit any reflections from these surfaces. The source had a
185 size of 1 mm, resembling the pencil lead used during the experiments, and was placed at 10 mm from the closest
186 sensor. A single sine cycle was emitted with a frequency of 450 kHz, being the peak frequency of the experimental
187 sensors. A set of sensors with a size of 5 mm, equal to the size of the pico sensors, was placed on the surface,
188 separated by a distance of 30 mm. The spatial resolution of the geometry was equal to 0.05 mm and the simulation
189 time was set at 100 μ s.



190

191 *Figure 4: Geometry of the simulation model, indicating the position of the source and sensors.*

192 Concerning the material properties allocated to the model, the characteristics of the reference mortar were used.
 193 The bulk density of the mortar was equal to 2170 kg/m^3 . From typical ultrasonic measurements performed on the
 194 identical mortar mixtures without steel reinforcement, an E-modulus of 27 GPa and a Poisson's ratio of 0.3 were
 195 found. For the steel reinforcement, a density of 7850 kg/m^3 , stiffness of 210 GPa and Poisson's ratio of 0.3 were
 196 inserted. Concerning damping coefficients for the mortar, these were adapted until an attenuation value of 0.32
 197 dB/mm, matching the experimental results (Appendix Table 1, attenuation for uncracked material) was reached. In
 198 case of the steel reinforcement, for which attenuation is expected negligible, the coefficients were chosen by the
 199 software's material database, resulting in an attenuation value of 0.03 dB/mm. Lastly, the crack was simulated by
 200 an air gap in the upper and lower layers of mortar, keeping the intact steel reinforcement in place (see dashed lines
 201 in Figure 4. The air gap was centred with respect to the sensors and had a width of $200 \mu\text{m}$. The properties of air
 202 were a density of 1.2 kg/m^3 and a longitudinal wave velocity of 330 m/s.

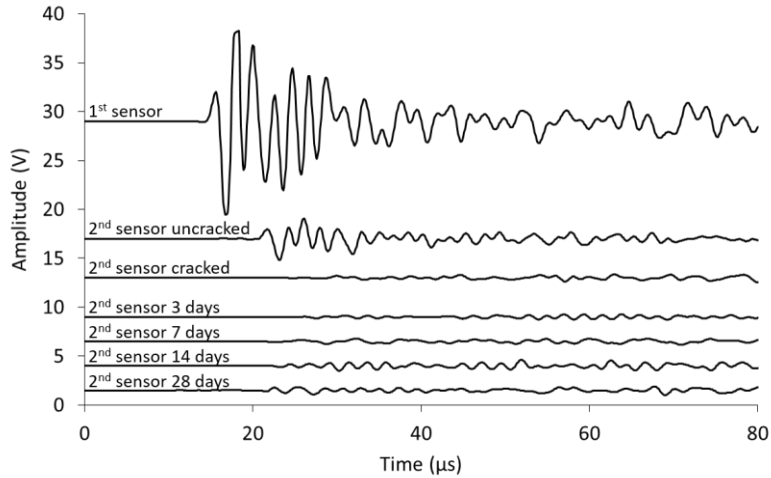
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204

205 **3. Results and discussion**

206 **3.1 Experimental series**

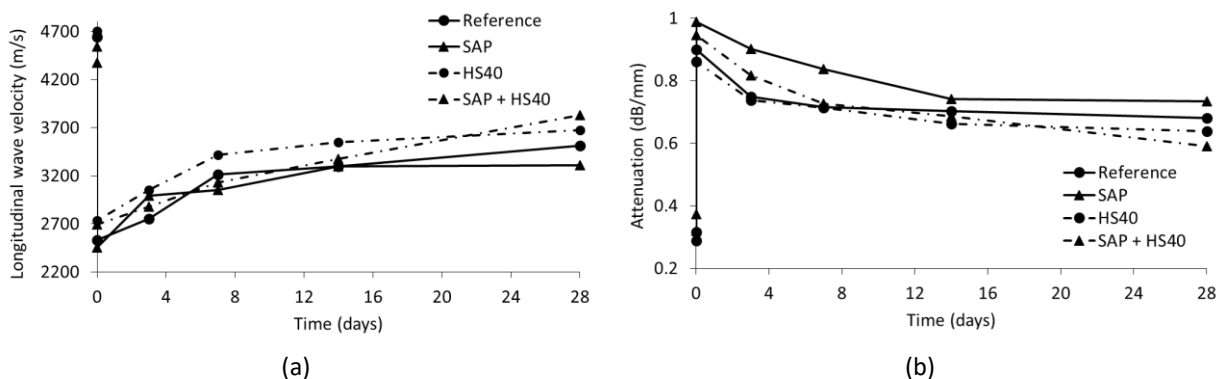
207 A global view on the evolution of the received waveforms throughout the experiments is studied. Figure 5 depicts
 208 the evolution of the waveforms of a representative reference specimen throughout the entire testing procedure.
 209 After cracking (2nd sensor cracked in Figure 5Figure 3), it was noticed that the waveform received by the sensor
 210 positioned after the discontinuity with respect to the excitation signal (see Figure 2) showed a strong decrease in
 211 amplitude compared to the uncracked situation. The created discontinuity within the travel path practically
 212 prohibited the wave to pass to the second sensor. Additionally, the Rayleigh cycle can no longer be identified, due
 213 to the loss of shear rigidity upon cracking. The specimen was then placed in wet-dry cycling, in order to promote the
 214 self-healing mechanism. Looking at the evolution of the waveforms, a gradual restoration of the amplitude values,
 215 as well as of the travel time can be observed between 3 and 28 days of healing. This partial amplitude restoration
 216 and transit time decrease suggest that partial crack closure occurred.



217

218 *Figure 5: Evolution of the waveforms during wet-dry curing of a representative reference specimen. The waveforms are shifted*
 219 *upwards for clarity.*

220 An analysis of the longitudinal wave velocity and attenuation was performed. The values shown in Figure 6 represent
 221 the average of all ultrasonic measurements conducted for each mixture series, being five pencil lead breaks per
 222 crack, for a total of three to six monitored cracks. The standard deviations are not included in the graphical
 223 representations below, in order to increase the comprehensibility of the observed trends. However, Appendix Table
 224 1 summarizes the experimental results and their coefficient of variation. In Figure 6 (a), the changes in the
 225 longitudinal wave velocity are presented with respect to the time. At day 0, two measurements per mixture
 226 composition were performed, being one in the uncracked state and one in cracked conditions. Velocities in between
 227 4300 and 4700 m/s were obtained before cracking, indicating a good quality of the mixtures [37]. However, the
 228 mortar blends with SAPs show lower velocities compared to the reference material, due to the increased
 229 macroscopic porosity. As expected, the crack creation lowered the velocity drastically, as the discontinuity
 230 prohibited the signal to follow the shortest path between both sensors. The wave could only reach the second sensor
 231 through locally present contact points between the crack walls, caused by crushed debris during unloading, or
 232 through refraction from the tip of the crack at the position of the reinforcement bar, something that noticeably
 233 increases the travel distance. During healing, the longitudinal wave velocity increased again, leading to a partial
 234 restoration of the original velocity value. From Figure 6 (a), a more pronounced improvement during the first week
 235 was detected for reference, SAP and HS40 mixtures, while the combination of SAPs and nanosilica demonstrated a
 236 more continuous increase over the entire healing period. This phenomenon will be clarified later upon discussion of
 237 the exact numbers. Nevertheless, the increment in wave velocity suggested partial healing for all tested mixtures.



238 *Figure 6: Evolution of (a) longitudinal wave velocity and (b) attenuation vs. time.*

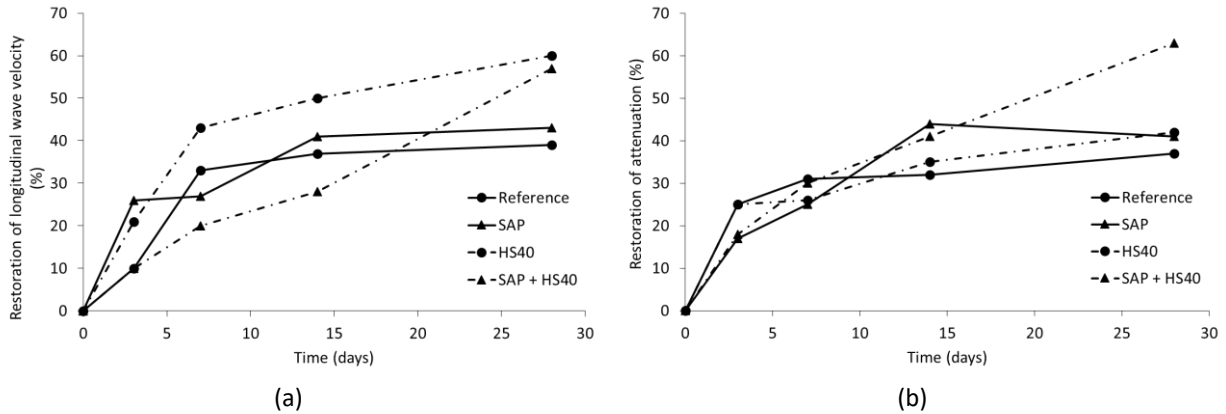
239 Figure 6 (b) depicts the development of the attenuation over time. Initially, the attenuation was relatively low,
240 though higher for the SAP mortar compared to the other mixtures. The introduction of the crack posed a
241 discontinuity within the matrix, which strongly increased the attenuation, from approximately 0.3 dB/mm to almost
242 1 dB/mm. Again, the application of wet-dry curing cycles partially restored the attenuation values, yielding a
243 significant reduction in attenuation within the first three to seven days of healing and a more gradual decrease
244 afterwards. The mortar with SAPs and HS40 showed a more continuous decrease in attenuation with respect to the
245 other mixtures.

246 To allow for a more thorough comparison between the different mixtures, the restoration in terms of velocity and
247 attenuation were calculated and are presented in Figure 7. This property was defined as the difference between the
248 healed and the cracked parameter values, compared to the degradation of this parameter upon cracking, and was
249 calculated using Equation 2:

$$Restoration [\%] = \frac{Q_{av.,healed} - Q_{av.,cracked}}{Q_{av.,uncracked} - Q_{av.,cracked}} * 100 \quad [2]$$

250

251 where $Q_{av.,x}$ signifies the average of the parameter under study, namely the wave velocity or attenuation, at stage X
252 (uncracked, cracked or healed). The exact values, together with the standard deviation between the three
253 specimens, are summarized in Appendix Table 1. The restoration of the longitudinal wave velocity, detailed in Figure
254 7 (a), showed an increase for all studied mixtures. However, some discrepancies between the mixture compositions
255 can be observed. In case of the reference, a restoration of about 10% was obtained during the first three days of
256 wet-dry curing. A continuation of these cycles then showed a further improvement to 33% after seven days of
257 healing, which indicates that further hydration and precipitation of $CaCO_3$ occurred, thanks to the regular water
258 supply through wet-dry curing. Yet, after 14 days of wet-dry cycles, the improvement slowed down, most likely due
259 to a shortage of unhydrated cement and $Ca(OH)_2$. A similar evolution was observed for the restoration of the
260 attenuation (Figure 7 (b)), which increased strongly during the first week of healing and stagnated afterwards. On
261 the other hand, the SAP mortar demonstrated a significant improvement in terms of velocity within the first three
262 days of curing, which can be attributed to the prolonged water supply. Afterwards, the recovery slowed down and
263 a slightly higher restoration percentage compared to the reference was obtained. The inclusion of nanosilica
264 contributes to autogenous healing by its pozzolanic reaction with $Ca(OH)_2$. During the first three days of wet-dry
265 curing, a recovery of the longitudinal velocity equal to 21% was noticed, showing an improvement compared to the
266 reference, but less effective than the addition of SAPs. Between three and seven days of healing, the restoration
267 percentage increased more strongly, i.e. from 21% to 43%. Most likely, the continued hydration that occurred upon
268 the placement in wet-dry curing cycles led to the formation of $Ca(OH)_2$ inside the crack, which then reacted with
269 nanosilica to form CSH. Lastly, the combination of SAPs and HS40 revealed a slow development of the healing process
270 during the first three healing days. Afterwards, the recovery accelerated and a considerable restoration percentage
271 of 57% was obtained after 28 days of wet-dry curing in terms of wave velocity and 63% in terms of attenuation.
272 These results confirm the inherent self-healing ability of cementitious mixtures without additives and acknowledge
273 the benefit of SAPs and nanosilica for the promotion of self-healing.



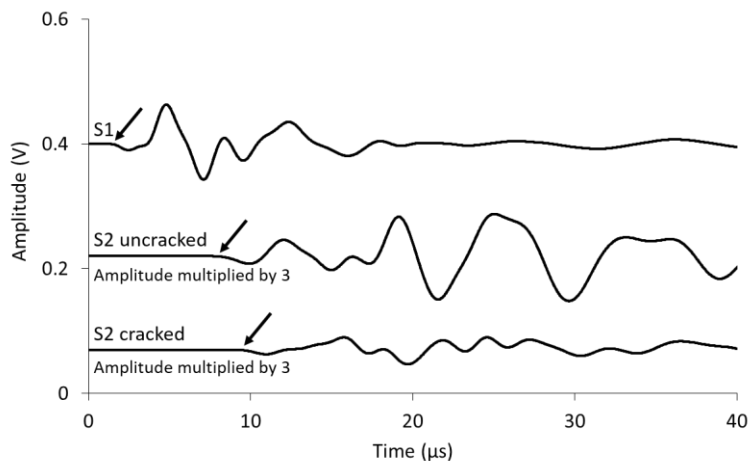
274 *Figure 7: Restoration of (a) longitudinal wave velocity and (b) attenuation after healing vs. time.*

275 The restoration of the wave parameters during wet-dry curing implies a certain change in the wave's travel path, as
 276 well as the existence of physical compounds inside the crack. Still, these parameters do not allow for a quantification
 277 of the actual filling of the crack, neither of the stiffness of the self-healing compounds. To get an insight in these
 278 features, numerical simulations are of paramount importance.

279

280 3.2 Numerical simulations

281 Figure 8 depicts the simulated waveforms captured by the sensors in the uncracked and cracked state. The upper
 282 waveform represents the signal received by the closest sensor. The arrival at the 2nd sensor corresponds to a wave
 283 velocity of 4615 m/s, similar to the experiments. The amplitude in the second sensor has decreased compared to
 284 the one in the first sensor, also seen during the experiments, leading to an attenuation of 0.32 dB/mm. Next, the air
 285 gap was created in between the two sensors with a thickness of 200 μm , going through the mortar solely, to simulate
 286 the crack. Similar to the conducted measurements, the arrival time was delayed resulting in a decrease of the
 287 longitudinal wave velocity by about 800 m/s, leading to a value of 3845 m/s after cracking. In addition, the
 288 attenuation was largely increased compared to the uncracked situation, increasing from 0.32 dB/mm to 0.65 dB/mm.



289

290 *Figure 8: Waveforms received from the numerical simulations. The waveforms are shifted upwards for clarity. The arrows*
 291 *indicate the arrival of the longitudinal wave.*

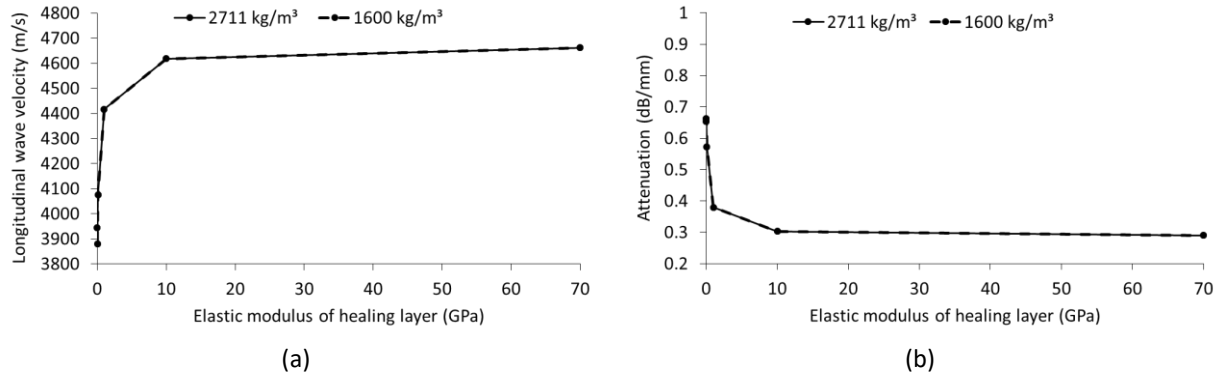
292 After the crack creation, the effect of filling the crack space was studied. For the numerical simulations, two
293 indicative cases of healing were considered, specifically a partially healed and a completely healed crack, depicted
294 in Figure 9. In case of a partially healed crack, a healing layer was placed within the top and bottom 3 mm of the
295 crack, while in deeper layers, closer to the reinforcement bar, the air gap was maintained. This specific healing case
296 was considered as it was reported in literature that autogenous healing mostly takes place close to the surface [38]
297 [32]. The completely healed situation concerns the filling of the entire crack with healing material.



298 *Figure 9: Representation of (a) partially healed and (b) completely healed simulation cases.*

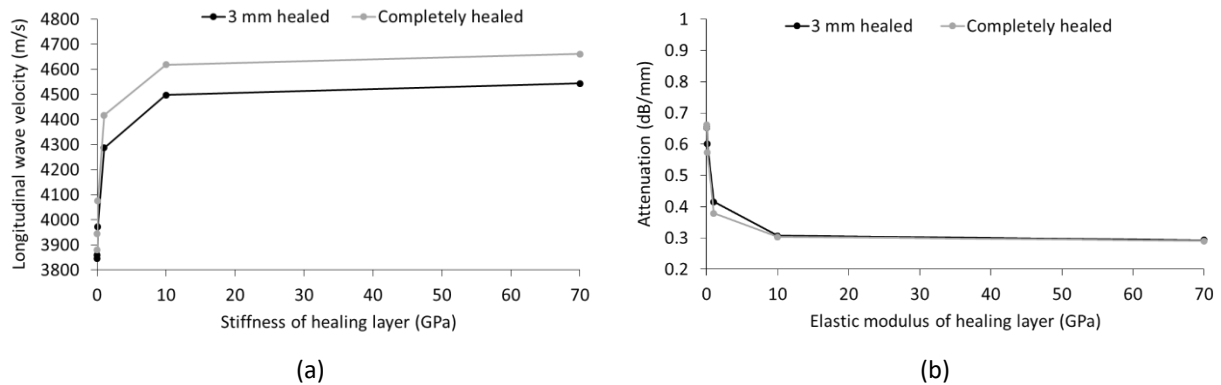
299 In order to model the process of self-healing, the basic properties of the healing material were varied, namely elastic
300 modulus and density. Regarding the E-modulus, 5 different cases were simulated, being 0.01 GPa, 0.1 GPa, 1 GPa,
301 10 GPa and 70 GPa. This selection spans all possible orders of magnitude of stiffness from nearly negligible to the
302 ideal stiffness of pure CaCO_3 crystals, which are abundantly formed throughout the autogenous healing process [38],
303 even though practically this value is not expected to be achieved within the narrow crack. Besides, it was decided to
304 use two density values, namely 2711 kg/m^3 (equal to the density of pure CaCO_3 in accordance to above) and 1600
305 kg/m^3 , which is notably lower than the ideal situation to account for the likely possibility that the healing will result
306 in compounds that deviate from the ideal condition. Nevertheless, it will be seen that the density only had a marginal
307 effect on the results.

308 First, the results of the completely healed situation are discussed. Figure 10 (a) depicts the longitudinal wave velocity
309 obtained. It was observed that the variation of the healing products' stiffness strongly affected the wave velocity.
310 Additionally, within the range of low stiffness values, the velocity increased steeply, whereas between 1 GPa and 10
311 GPa, and later between 10 GPa and 70 GPa, the slope was reduced. These results indicate that the filling of the crack,
312 even with a low-stiffness material, influences the propagation of ultrasonic waves significantly. Also, the original
313 velocity before cracking, i.e. about 4615 m/s, should be reached between 10 GPa and 70 GPa. These trends were
314 visible for both densities used. The effect of variable density on the simulated wave velocity was below 1%, making
315 no practical difference. The attenuation values obtained from the fully healed simulation model are presented in
316 Figure 10 (b). The attenuation varied between 0.65 dB/mm in the cracked state and 0.29 dB/mm in case of pure
317 CaCO_3 filling, showing the decreasing trend of attenuation with stiffness. The reduction was more pronounced up to
318 1 GPa, while the decrease slowed down afterwards. Also, the attenuation obtained for a stiffness of 10 GPa and 70
319 GPa was lower than the attenuation of 0.32 dB/mm seen for the uncracked situation, meaning that a complete
320 recovery was obtained.



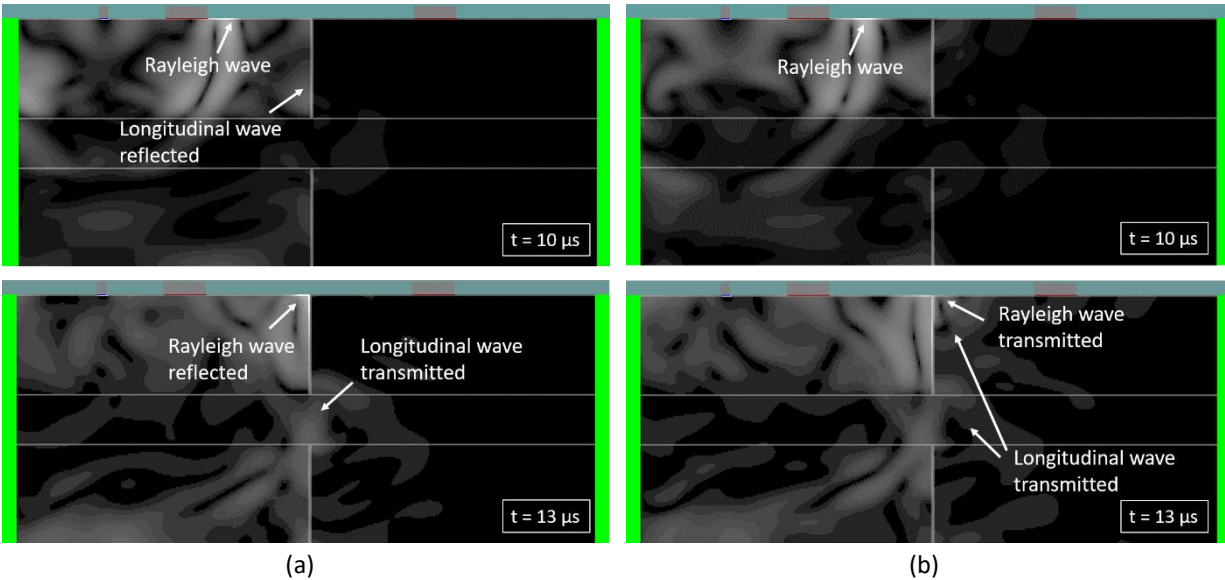
321 *Figure 10: (a) Longitudinal velocity and (b) attenuation vs. elastic modulus of the healing layer in case of complete healing for*
 322 *densities of 1600 kg/m³ and 2711 kg/m³.*

323 Next, the simulation results with a partially healed crack are presented. As the density showed to only have a
 324 marginal influence on the outcome, the different densities will not be discussed in-depth. Figure 11 shows the
 325 partially and completely healed stages, having a healing layer density of 1600 kg/m³. The longitudinal velocity (see
 326 Figure 11 (a)) showed a similar development compared to the completely healed case, being approximately 3% lower
 327 for the partial healing. Concerning the attenuation, the results in Figure 11 (b) were closely related to the completely
 328 healed situation. A slightly increased attenuation was seen up to a stiffness of 1 GPa, after which nearly identical
 329 values were reached. These results indicate that, in terms of attenuation, partial healing is sufficient to restore the
 330 wave propagation as measured with this main frequency (450 kHz) and this sensor size (5 mm).



331 *Figure 11: (a) Longitudinal velocity and (b) attenuation vs. elastic modulus of the healing layer in case of a partially and*
 332 *completely healed crack.*

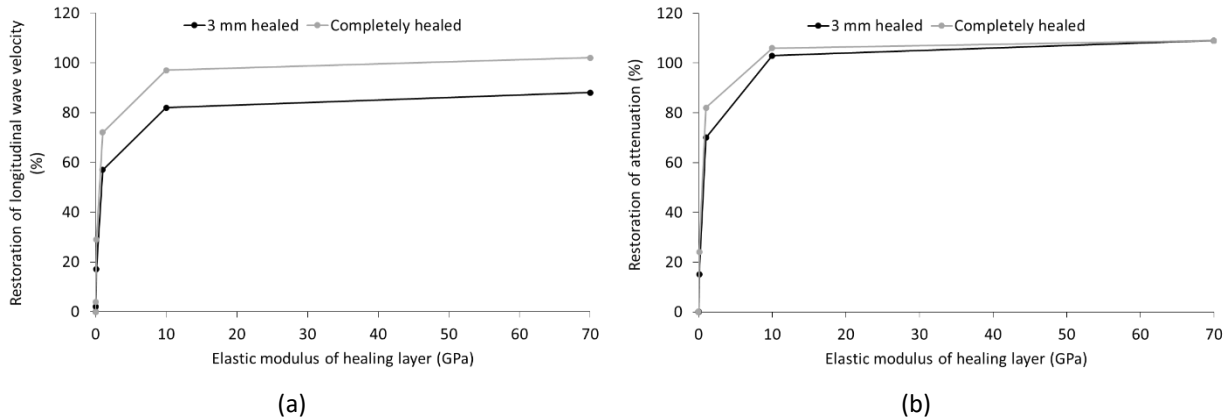
333 The snapshots of the transient displacement fields in Figure 12 (a) and (b) reveal the wave propagation path at
 334 different timings during the numerical simulations in the cracked and partially healed stages, respectively. In the
 335 cracked situation (a), the wave was mostly reflected onto the boundary of the created air gap, whereas only a small
 336 part of the signal was able to pass to the second sensor through the crack tip on top of the steel reinforcement. The
 337 surface or Rayleigh wave was completely reflected onto the crack opening. Concerning the partially healed situation,
 338 the simulations demonstrated the transmission of both the longitudinal and the Rayleigh wave through the healing
 339 layer inserted at the top of the crack, which led to a shortened travel path and thus an increased wave velocity and
 340 amplitude.



341 *Figure 12: Snapshots of the wave simulations in (a) cracked stage and (b) partially healed situation with an elastic modulus of 10*
 342 *GPa. The green boundaries signify infinite boundary conditions.*

343 The numerical results demonstrate the excellent sensitivity of ultrasound to the stiffness of the healing layer,
 344 especially at the crucial initial phase where the stiffness develops from practically zero to 1 GPa. Within this region
 345 of developing stiffness values, the velocity showed an increase up to 550 m/s, which equals 12% of the uncracked
 346 velocity. Still, even for later increases in stiffness from 1 GPa to 10 GPa, the longitudinal wave velocity increased by
 347 approximately 200 m/s. A similar, even more pronounced, trend can be seen for the attenuation, as the relative
 348 decrease between 1 GPa and 10 GPa amounts to 19% and is mostly attributed to the reduced reflection between
 349 the mortar and the stiffening healing compounds.

350 Finally, the restoration percentages obtained from the numerical simulations are summarized in Figure 13. A table
 351 summarizing the exact values for a density of 1600 kg/m³ can be found in the Appendix. Regarding the restoration
 352 of the longitudinal wave velocity, a similar, increasing trend was observed for both healing cases with increased
 353 stiffness of the healing layer. However, an improved recovery was seen for a completely filled crack, due to the
 354 increased transmission of the signal. Similarly, the restoration of the attenuation demonstrated an increasing value
 355 for higher stiffness of the healing layer, i.e. up to 109%. When comparing the outcome of a 3 mm healing layer to a
 356 completely healed crack, the restoration was noticeably different for low stiffness values only (up to 1 GPa). At higher
 357 stiffness, the restoration percentage was approximately identical, meaning that stiff healing compounds close to the
 358 surface can restore the attenuation as measured for this frequency and sensor size. The Rayleigh wavelength,
 359 calculated by the Rayleigh velocity (approximately 2500 m/s) divided by the basic signal frequency of 450 kHz, is
 360 equal to 5.5 mm. Therefore, for the specific experimental case, most of the energy would anyway propagate through
 361 a shallow layer, also seen in [39]. The distinction between partial and complete healing is thus not expected to be
 362 straightforward. However, lower frequencies, yielding deeper penetration, could be used to characterize the filling
 363 percentage.



364 *Figure 13: Restoration of (a) longitudinal wave velocity and (b) attenuation vs. elastic modulus of the healing layer for partially*
 365 *and completely healed simulation stages.*

366 During the experimental series, a recovery of the longitudinal wave velocity up to 43% was noticed in case of a
 367 mortar including SAPs and even 60% for the addition of nanosilica, indicating a considerable crack filling effect.
 368 Considering the restoration based on the simulations, as shown in Figure 13, a restoration percentage of 43%
 369 matched the range of healing stiffness between 0.1 GPa and 1 GPa, in case of both partial and complete healing,
 370 whereas 60% restoration is situated between 0.1 GPa and 1 GPa for partial healing and between 1 GPa and 10 GPa
 371 for complete healing. These results thus suggest a relatively low stiffness of the formed healing layer, which seems
 372 likely if one considers the healing circumstances of the experimental series. Foremost, the mechanism of autogenous
 373 healing depends on multiple factors, such as the availability of unhydrated cement, $\text{Ca}(\text{OH})_2$ and moisture. When
 374 these components are absent or consumed, autogenous healing no longer takes places. Secondly, the mortar
 375 specimens were cracked by means of a tensile test, leading to multiple, through-going cracks. The only connection
 376 between the crack walls was the steel reinforcement bar, which was situated in the centre. The number of
 377 precipitation surfaces was therefore limited, while literature demonstrated the benefit of having a high amount of
 378 precipitation surfaces, which can be accomplished by the addition of fibres [40]. These reasons imply that the order
 379 of stiffness of the healing products is certainly lower than the mortar itself, something in agreement with the
 380 restoration of wave parameters. The ultrasonic surface wave measurements thus showed to be valuable to assess
 381 the closure of the cracks, while the combination with the numerical simulations allowed for a non-destructive
 382 estimation of the stiffness of the healing layer for the first time in literature.

383
 384 **3. Conclusion**

385 Within this study, the self-healing effectiveness of cementitious mortars was assessed by means of surface ultrasonic
 386 wave measurements. To promote autogenous healing, superabsorbent polymers and nanosilica were added to the
 387 mixtures and wet-dry curing was applied. Through an analysis of the longitudinal wave velocity and the attenuation,
 388 the evolution of the crack healing was evaluated, demonstrating a partial restoration of these parameters for all
 389 mixtures, after the initial significant change due to cracking. Whereas comparable trends were noticed for each
 390 mixture composition, the blends with SAPs and/or nanosilica showed an improved recovery of the wave parameters.

391 Besides the conducted experiments, numerical simulations were performed to validate the sensitivity of ultrasound
 392 to a developing healing layer. Whereas the density of the healing layer only marginally influenced the obtained wave
 393 parameters, a significant recovery of the longitudinal wave velocity and attenuation was observed for elastic moduli
 394 within the range of 0.01 GPa and 1 GPa, while still being measurable for higher stiffnesses between 1 GPa and 70
 395 GPa. This validates the sensitivity of US to the stiffness development within the healing layer and its characterization
 396 potential for self-healing composites. Besides, a comparison between a partially and completely filled crack

397 demonstrated a noticeably higher velocity in case of complete filling, while the attenuation showed to differ for low
398 stiffness values (below 10 GPa) only. The latter was ascribed to the specific conditions of the measurements, utilizing
399 a frequency of 450 kHz, which limits the possibility to differentiate between partial and complete healing. For this
400 reason, different excitation frequencies could supply a solution, since they define the penetration depth of the
401 Rayleigh waves. In addition, ultrasonic mapping using transmission measurements would prove useful, disclosing
402 the improvements within the entire crack cross-section.

403 The combination of experiments and simulations points to a measurable recovery due to self-healing, while exposing
404 the relatively low stiffness of the healing products, i.e. mostly between 0.1 GPa and 1 GPa, based on the relative
405 restoration. It should be highlighted that the importance of this study lies in the disclosure of the sensitivity of
406 different wave parameters to the existence of a crack and healing, rather than to exactly match the experimental
407 and numerical values during the whole process. Discrepancies were noticed in terms of exact values and can be
408 explained by the differences between the simulated geometry and the actual specimens. In the numerical
409 simulations, a 2D representation of the set-up is used and the attenuation was fitted to the experimental one, to
410 account for damping as well as spreading of the beam. However, it is supposed that 3D simulations could be more
411 appropriate to accommodate the actual 3D spreading of the wave beam. Additionally, the discussion of wave velocity
412 focused on the longitudinal wave, since the Rayleigh cycle was not identified after cracking. The first observable
413 disturbance is always attributed to longitudinal waves, either directly transmitted (uncracked case) or through
414 contact points (cracked and healed cases). However, attenuation can be considered as a measure of the total
415 transmission. In the intact state, the peak amplitude at both sensors can be safely attributed to Rayleigh waves, as
416 seen for example in Figure 3. However, for latter cases, and especially the first measurement after cracking, Rayleigh
417 waves were not identified as already discussed. Therefore, even though the attenuation is not attributed to the
418 Rayleigh cycle, it is still a parameter that monotonically changes with healing and can be used for the evaluation of
419 the process. Another point related to ultrasound is that the size of the sensors is known to influence the amplitude
420 through the "aperture effect" [41] [42]. This effect is stronger for surface waves and was inevitably included in the
421 experimental measurements. Therefore, although numerical simulations with smaller, point sensors are possible,
422 simulations from 5 mm sensors were presented to exercise the same aperture effect with the experiment. The
423 present study confirms the potential of ultrasonic monitoring for self-healing purposes. The combination with
424 numerical simulations allowed to estimate the stiffness of the formed healing products and paves the way for
425 ultrasound to be used for self-healing evaluation.

426

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430

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432

433 *Appendix Table 1: Longitudinal wave velocity (m/s), restoration of longitudinal wave velocity after healing (%), attenuation*
 434 *(dB/mm) and restoration of attenuation after healing (%) of the mortar mixtures in the cracked, uncracked and healed stages,*
 435 *together with the coefficient of variation (n = 3).*

		Longitudinal wave velocity (m/s)	Restoration of longitudinal wave velocity after healing (%)	Attenuation (dB/mm)	Restoration of attenuation after healing (%)
Reference	Uncracked	4647 ± 7%	n/a	0.32 ± 31%	n/a
	Cracked	2534 ± 12%	n/a	0.90 ± 20%	n/a
	3 days	2753 ± 17%	10 ± 130%	0.75 ± 16%	25 ± 8%
	7 days	3215 ± 11%	33 ± 24%	0.72 ± 29%	31 ± 10%
	14 days	3269 ± 15%	37 ± 54%	0.70 ± 20%	32 ± 60%
	28 days	3378 ± 3%	39 ± 8 %	0.68 ± 13%	37 ± 24%
SAP	Uncracked	4376 ± 6%	n/a	0.37 ± 38%	n/a
	Cracked	2452 ± 10%	n/a	0.99 ± 12%	n/a
	3 days	2994 ± 13%	26 ± 35%	0.90 ± 17%	17 ± 71%
	7 days	3051 ± 9%	27 ± 67%	0.84 ± 17%	25 ± 16%
	14 days	3297 ± 10%	41 ± 29%	0.74 ± 14%	44 ± 30%
	28 days	3311 ± 6%	43 ± 2%	0.73 ± 10%	41 ± 15%
HS40	Uncracked	4703 ± 12%	n/a	0.29 ± 41%	n/a
	Cracked	2733 ± 10%	n/a	0.86 ± 29%	n/a
	3 days	3051 ± 14%	21 ± 110%	0.74 ± 23%	25 ± 92%
	7 days	3419 ± 7%	43 ± 67%	0.71 ± 27%	26 ± 12%
	14 days	3548 ± 7%	50 ± 48%	0.66 ± 17%	35 ± 37%
	28 days	3677 ± 7%	60 ± 55%	0.62 ± 27%	42 ± 57%
SAP + HS40	Uncracked	4542 ± 8%	n/a	0.32 ± 38%	n/a
	Cracked	2694 ± 7%	n/a	0.95 ± 19%	n/a
	3 days	2878 ± 7%	10 ± 50%	0.82 ± 17%	18 ± 72%
	7 days	3128 ± 9%	20 ± 35%	0.73 ± 34%	30 ± 43%
	14 days	3374 ± 11%	28 ± 39%	0.69 ± 16%	41 ± 10%
	28 days	3832 ± 4%	57 ± 14%	0.59 ± 19%	63 ± 22%

436

437 *Appendix Table 2: Longitudinal wave velocity (m/s), restoration of longitudinal wave velocity after healing (%), attenuation*
 438 *(dB/mm) and restoration of attenuation after healing (%) of the numerical simulations for partial and complete healing and*
 439 *varying stiffness of the healing layer.*

		Longitudinal wave velocity (m/s)	Restoration of longitudinal wave velocity after healing (%)	Attenuation (dB/mm)	Restoration of attenuation after healing (%)
	Uncracked	4645	n/a	0.32	n/a
	Cracked	3845	n/a	0.65	n/a
	0.01 GPa	3860	2	0.65	0
3 mm healed	0.1 GPa	3977	17	0.60	15
	1 GPa	4302	57	0.42	70
	10 GPa	4502	82	0.31	103
	70 GPa	4549	88	0.29	109
	0.01 GPa	3879	4	0.66	-3
Fully healed	0.1 GPa	4075	29	0.57	24
	1 GPa	4417	72	0.38	82
	10 GPa	4618	97	0.30	106
	70 GPa	4662	102	0.29	109

440